An introduction to MPI



(word cloud of all the MPI hydro code written for this course: http://www.wordle.net)

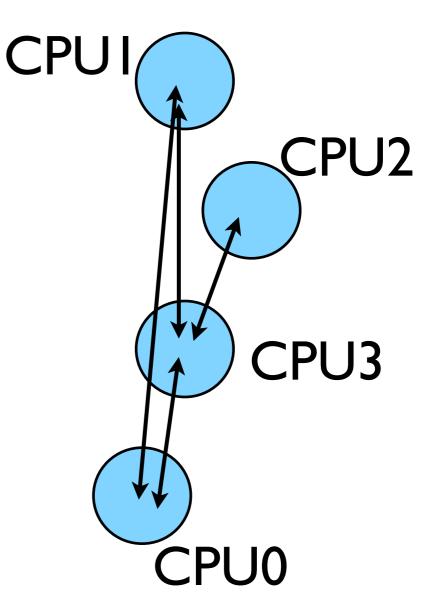
MPI is a **Library** for Message-Passing

- Not built in to compiler
- Function calls that can be made from any compiler, many languages
- Just link to it
- Wrappers: mpicc, mpif77

```
#include <stdio.h>
#include <mpi.h>
int main(int argc, char **argv) {
    int rank, size;
   MPI_Init(&argc, &argv);
   MPI_Comm_size(MPI_COMM_WORLD, &size);
    MPI_Comm_rank(MPI_COMM_WORLD, &rank);
    printf("Hello, world, from task %d of %d!\
           rank, size);
    MPI_Finalize();
    return 0;
program helloworld
                                   Fortran
use mpi
implicit none
integer :: rank, comsize, ierr
call MPI_Init(ierr)
call MPI_Comm_size(MPI_COMM_WORLD, comsize, i
call MPI_Comm_rank(MPI_COMM_WORLD, rank, ierr
print *, 'Hello world, from task ', rank, &
         of ', comsize
call MPI_Finalize(ierr)
end program helloworld
```

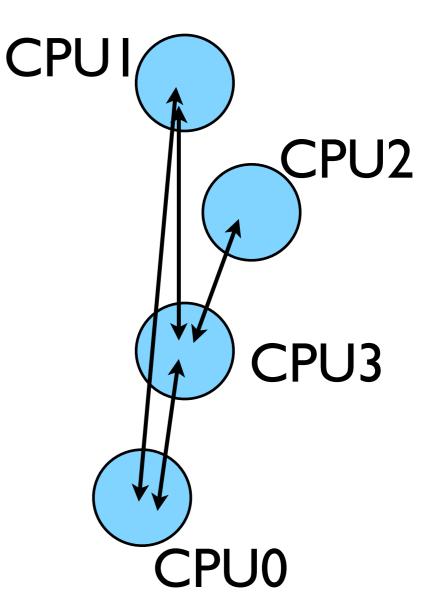
MPI is a Library for **Message-Passing**

- Communication/coordination between tasks done by sending and receiving messages.
- Each message involves a function call from each of the programs.



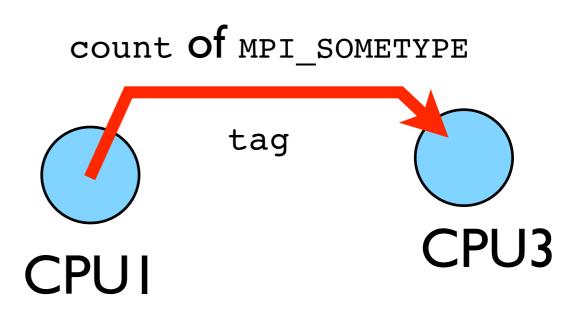
MPI is a Library for **Message-Passing**

- Three basic sets of functionality:
 - Pairwise communications via messages
 - Collective operations via messages
 - Efficient routines for getting data from memory into messages and vice versa



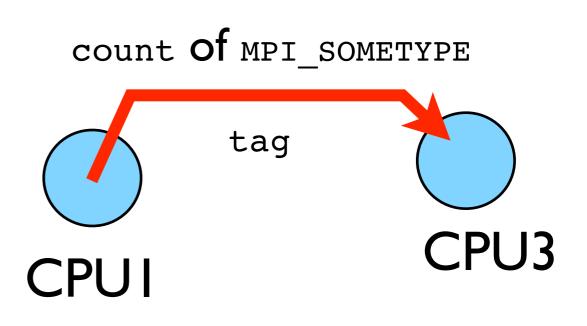
Messages

- Messages have a sender and a receiver
- When you are sending a message, don't need to specify sender (it's the current processor),
- A sent message has to be actively received by the receiving process



Messages

- MPI messages are a string of length count all of some fixed MPI type
- MPI types exist for characters, integers, floating point numbers, etc.
- An arbitrary integer tag is also included - helps keep things straight if lots of messages are sent.



Size of MPI Library

- Many, many functions (>200)
- Not nearly so many concepts
- We'll get started with just 10-12, use more as needed.

MPI_Init()
MPI_Comm_size()
MPI_Comm_rank()
MPI_Ssend()
MPI_Recv()
MPI_Finalize()

Hello World

- The obligatory starting point
- cd ~/ppp/mpi-intro
- Type it in, compile and run it together

```
program helloworld
use mpi
implicit none
integer :: rank, comsize, ierr
call MPI_Init(ierr)
call MPI_Comm_size(MPI_COMM_WORLD, comsize, ierr)
call MPI_Comm_rank(MPI_COMM_WORLD, rank, ierr)
print *,'Hello world, from task ', rank, &
        ' of ', comsize
call MPI_Finalize(ierr)
end program helloworld
```

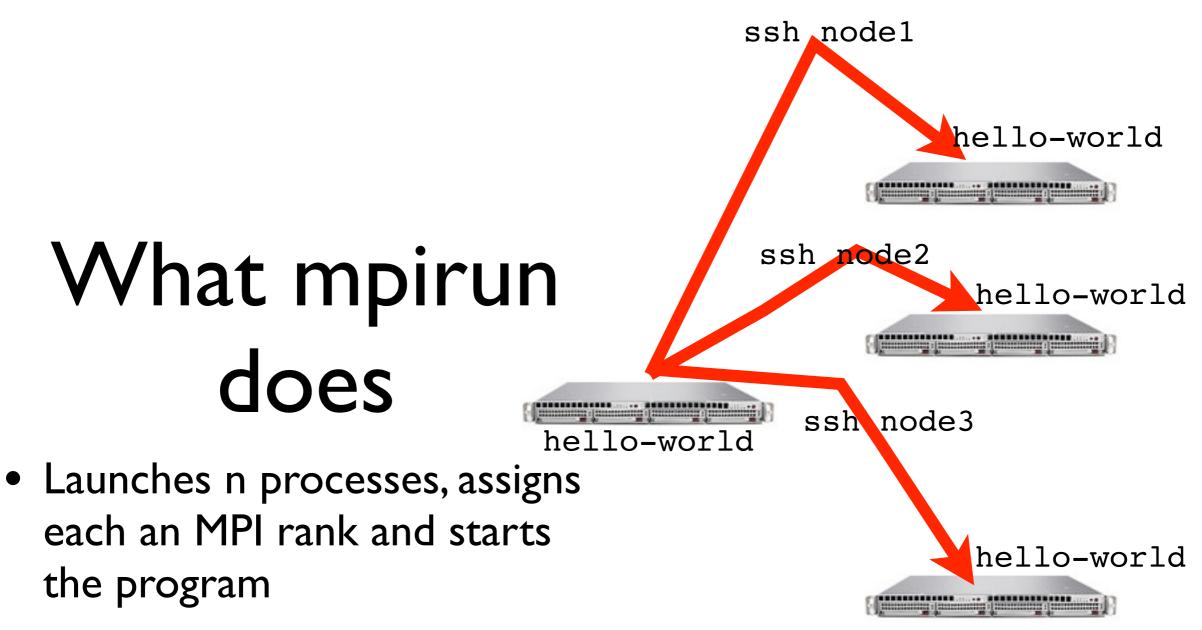
#include <stdio.h> C
#include <mpi.h> C
int main(int argc, char **argv) {
 int rank, size;
 MPI_Init(&argc, &argv);
 MPI_Comm_size(MPI_COMM_WORLD, &size);
 MPI_Comm_rank(MPI_COMM_WORLD, &rank);
 printf("Hello, world, from task %d of %d!\n",
 rank, size);
 MPI_Finalize();
 return 0;
}

What mpicc/ mpif77 do

- Just wrappers for the system C, Fortran compilers that have the various -I, -L clauses in there automaticaly
- -v option (sharcnet) or
 --showme (OpenMPI) shows which options are being used

\$ mpicc --showme hello-world.c
-o hello-world

gcc -I/usr/local/include -pthread hello-world.c -o hello-world -L/usr/local/lib -lmpi -lopen-rte -lopen-pal -ldl -Wl,--export-dynamic -lnsl -lutil -lm -ldl



 For multinode run, has a list of nodes, ssh's to each node and launches the program

Number of Processes

- Number of processes to use is almost always equal to the number of processors
- But not necessarily.
- On your nodes, what happens when you run this?

\$ mpirun -np 24 hello-world

mpirun runs any program

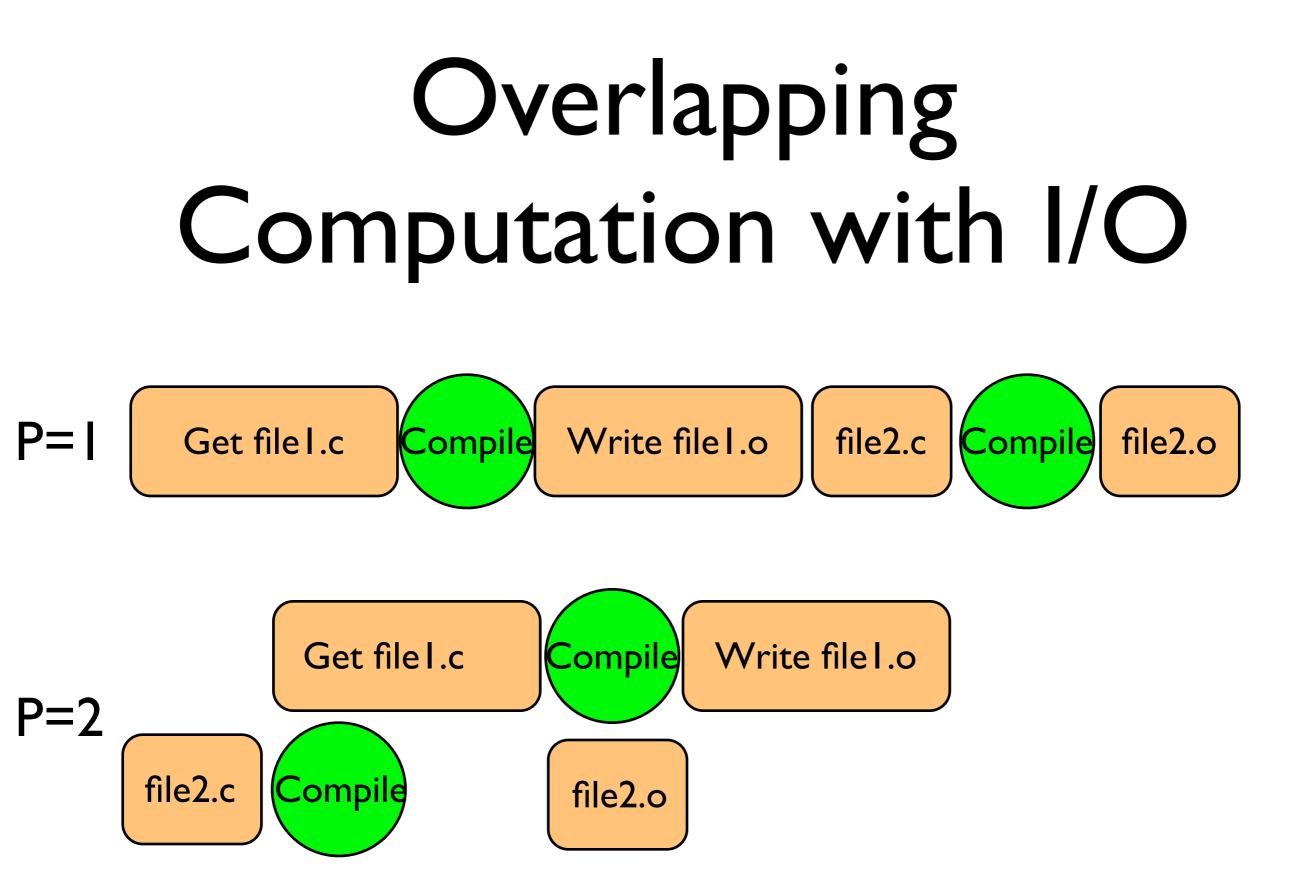
- mpirun will start that processlaunching procedure for any progam
- Sets variables somehow that mpi programs recognize so that they know which process they are

```
$ hostname
$ mpirun -np 4 hostname
$ ls
$ mpirun -np 4 ls
```

make

- Make builds an executable from a list of source code files and rules
- Many files to do, of which order doesn't matter for most
- Parallelism!
- make -j N launches N processes to do it
- make -j 2 often shows speed increase even on single processor systems

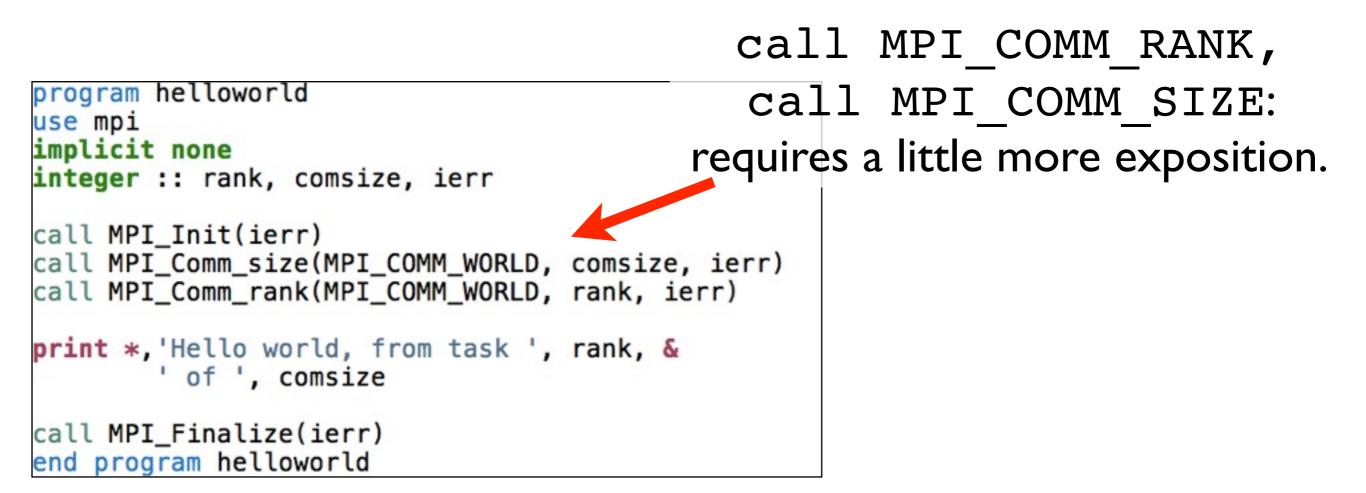
\$ make \$ make -j 2 \$ make -j



What the code does

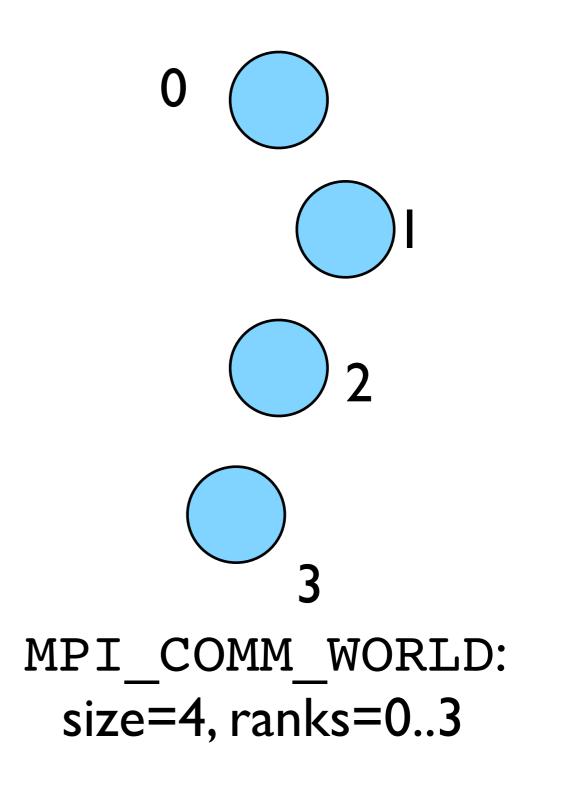
• (FORTRAN version; C is similar)

use mpi : imports declarations for MPI function calls program hellowork use mpi implicit none call MPI INIT(ierr): integer :: rank, comsize, ierr initialization for MPI library. call MPI_Init(ierr) call MPI_Comm_size(MPI_COMM_WORLD, comsize, Merr) call MPI_Comm_rank(MPI_COMM_WORLD, rank, ieMUSt come first. print *, 'Hello world, from task ', rank, & ierr: Returns any error code. ' of ', comsize call MPI_Finalize(ierr) end program helloworld call MPI FINALIZE(ierr): close up MPI stuff. Must come last. ierr: Returns any error code.



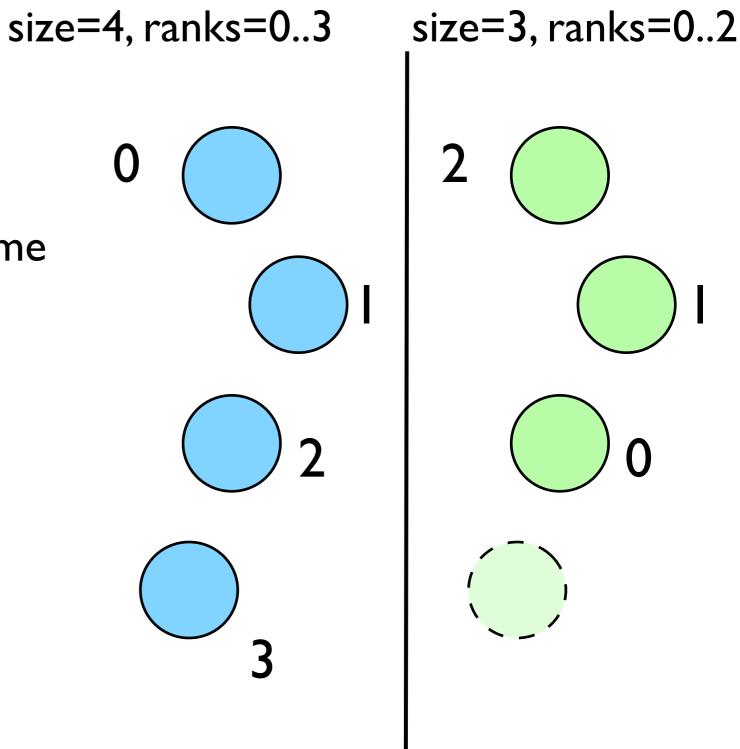
Communicators

- MPI groups processes into communicators.
- Each communicator has some size -- number of tasks.
- Each task has a rank 0..size-I
- Every task in your program belongs to MPI_COMM_WORLD



Communicators

- Can create our own communicators over the same tasks
- May break the tasks up into subgroups
- May just re-order them for some reason



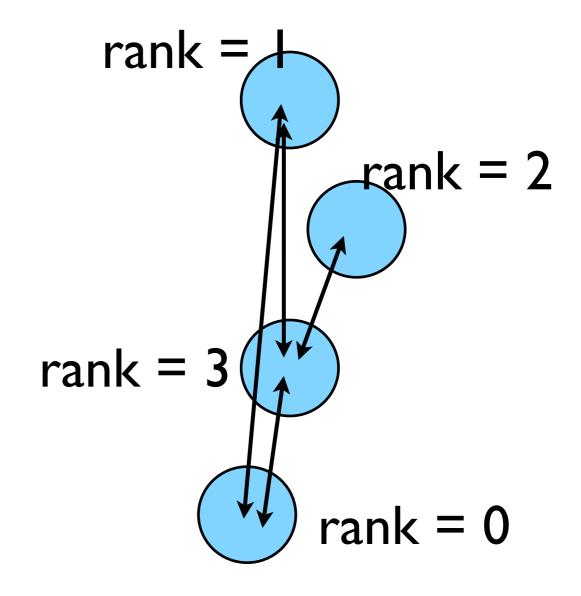
new comm

MPI COMM WORLD:



Rank and Size much more important in MPI than OpenMP

- In OpenMP, compiler assigns jobs to each thread; don't need to know which one you are.
- MPI: processes determine amongst themselves which piece of puzzle to work on, then communicate with appropriate others.



С	Fortran						
<pre>#include <stdio.h> #include <mpi.h></mpi.h></stdio.h></pre>	program helloworld use mpi						
<pre>int main(int argc, char **argv) { int rank, size;</pre>	<pre>implicit none integer :: rank, comsize, ierr</pre>						
<pre>MPI_Init(&argc, &argv); MPI_Comm_size(MPI_COMM_WORLD, &size); MPI_Comm_rank(MPI_COMM_WORLD, &rank);</pre>	<pre>call MPI_Init(ierr) call MPI_Comm_size(MPI_COMM_WORLD, comsize, i call MPI_Comm_rank(MPI_COMM_WORLD, rank, ierr</pre>						
<pre>printf("Hello, world, from task %d of %d!\n" rank, size);</pre>	<pre>print *, 'Hello world, from task ', rank, &</pre>						
<pre>MPI_Finalize(); return 0; }</pre>	call MPI_Finalize(ierr) end program helloworld						

- #include <mpi.h> vs use mpi
- C functions **return** ierr;
- Fortran **pass** ierr
- MPI_Init

Our first real MPI program - but no Ms are P'ed!

- Let's fix this
- mpicc -o firstmessage firstmessage.c
- mpirun -np 2 ./firstmessage

}

• Note: C - MPI_CHAR

```
#include <stdio.h>
#include <mpi.h>
int main(int argc, char **argv) {
    int rank, size, ierr;
    int sendto, recvfrom; /* task to send, recv from */
                        /* shared tag to label msgs*/
    int ourtag=1;
    char sendmessage[]="Hello";
                                    /* text to send */
    char getmessage[6]; /* text to recieve */
   MPI_Status rstatus; /* MPI_Recv status info */
    ierr = MPI_Init(&argc, &argv);
    ierr = MPI_Comm_size(MPI_COMM_WORLD, &size);
    ierr = MPI_Comm_rank(MPI_COMM_WORLD, &rank);
   if (rank == 0) {
       sendto = 1;
        ierr = MPI_Ssend(sendmessage, 6, MPI_CHAR, sendto,
                        ourtag, MPI_COMM_WORLD);
       printf("%d: Sent message <%s>\n", rank, sendmessage);
    } else if (rank == 1) {
        recvfrom = 0;
        ierr = MPI_Recv(getmessage, 6, MPI_CHAR, recvfrom,
                       ourtag, MPI_COMM_WORLD, &rstatus);
       printf("%d: Got message <%s>\n", rank, getmessage);
    ierr = MPI_Finalize();
    return 0;
```

Fortran version

- Let's fix this
- mpif90 -o
 firstmessage
 firstmessage.f90
- mpirun -np 2 ./ firstmessage
- FORTRAN -MPI_CHARACTER

```
program firstmessage
use mpi
implicit none
integer :: rank, comsize, ierr
integer :: sendto, recvfrom ! Task to send, recv from
character(5) :: sendmessage ! text to send
character(5) :: getmessage ! text rcvd
integer, dimension(MPI_STATUS_SIZE) :: rstatus
call MPI_Init(ierr)
call MPI_Comm_rank(MPI_COMM_WORLD, rank, ierr)
call MPI_Comm_size(MPI_COMM_WORLD, comsize, ierr)
if (rank == 0) then
   sendmessage = 'Hello'
   sendto = 1
   call MPI_Ssend(sendmessage, 5, MPI_CHARACTER, sendto, &
                 ourtag, MPI_COMM_WORLD, ierr)
   print *, rank, ' sent message <', sendmessage, '>'
else if (rank == 1) then
   recvfrom = 0
   call MPI_Recv(getmessage, 5, MPI_CHARACTER, recvfrom, &
                ourtag, MPI_COMM_WORLD, rstatus, ierr)
   print *, rank, ' got message <',getmessage,'>'
endif
```

```
call MPI_Finalize(ierr)
end program firstmessage
```

C - Send and Receive

MPI_Status status;

Fortran - Send and Receive

integer status(MPI_STATUS_SIZE)

call MPI_RECV(rcvarr, count, MPI_TYPE, source, tag, Communicator, status, ierr)

Special Source/Dest: MPI_PROC_NULL

MPI_PROC_NULL basically ignores the relevant operation; can lead to cleaner code.

Special Source: MPI_ANY_SOURCE

MPI_ANY_SOURCE is a wildcard; matches any source when receiving.

More complicated example:

 Let's look at secondmessage.f90, secondmessage.c

}

```
#include <stdio.h>
#include <mpi.h>
int main(int argc, char **argv) {
    int rank, size, ierr;
    int left, right;
    int tag=1;
    double msgsent, msgrcvd;
    MPI_Status rstatus;
    ierr = MPI_Init(&argc, &argv);
    ierr = MPI_Comm_size(MPI_COMM_WORLD, &size);
    ierr = MPI_Comm_rank(MPI_COMM_WORLD, &rank);
    left = rank -1;
    if (left < 0) left = MPI_PROC_NULL;</pre>
    right = rank + 1;
    if (right == size) right = MPI_PROC_NULL;
    msgsent = rank*rank;
    msgrcvd = -999;
    ierr = MPI_Ssend(&msgsent, 1, MPI_DOUBLE, right,
                     tag, MPI_COMM_WORLD);
    ierr = MPI_Recv(&msgrcvd, 1, MPI_DOUBLE, left,
                     tag, MPI_COMM_WORLD, &rstatus);
    printf("%d: Sent %lf and got %lf\n",
                rank, msgsent, msgrcvd);
    ierr = MPI_Finalize();
    return 0;
```

More complicated example:

 Let's look at secondmessage.f90, secondmessage.c

```
program secondmessage
use mpi
implicit none
integer :: ierr, rank, comsize
integer :: left, right
integer :: tag
integer :: status(MPI_STATUS_SIZE)
double precision :: msgsent, msgrcvd
call MPI_INIT(ierr)
call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
call MPI_COMM_SIZE(MPI_COMM_WORLD, comsize, ierr)
left = rank-1
if (left < 0) left = MPI_PROC_NULL</pre>
right = rank+1
if (right >= comsize) right = MPI_PROC_NULL
msgsent = rank*rank
msgrcvd = -999.
tag = 1
call MPI_Ssend(msgsent, 1, MPI_DOUBLE_PRECISION, right, &
               tag, MPI_COMM_WORLD, ierr)
call MPI_Recv(msgrcvd, 1, MPI_DOUBLE_PRECISION, left, &
               tag, MPI_COMM_WORLD, status, ierr)
print *, rank, 'Sent ', msgsent, 'and recvd ', msgrcvd
call MPI_FINALIZE(ierr)
end program secondmessage
```

Compile and run

- mpi{cc,f90} -o secondmessage secondmessage.{c,f90}
- mpirun -np 4 ./secondmessage

\$ mpirun -np 4 ./secondmessage
3: Sent 9.000000 and got 4.000000
0: Sent 0.000000 and got -999.000
1: Sent 1.000000 and got 0.000000
2: Sent 4.000000 and got 1.000000

```
#include <stdio.h>
#include <mpi.h>
```

```
int main(int argc, char **argv) {
    int rank, size, ierr;
    int left, right;
    int tag=1;
    double msgsent, msgrcvd;
    MPI_Status rstatus;
```

```
ierr = MPI_Init(&argc, &argv);
ierr = MPI_Comm_size(MPI_COMM_WORLD, &size);
ierr = MPI_Comm_rank(MPI_COMM_WORLD, &rank);
```

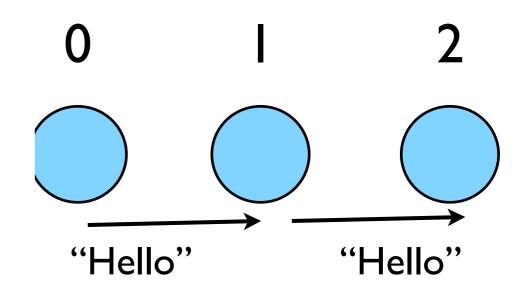
```
left = rank - 1;
if (left < 0) left = MPI_PROC_NULL;
right = rank + 1;
if (right == size) right = MPI_PROC_NULL;
```

```
msgsent = rank*rank;
msgrcvd = -999;
```

```
printf("%d: Sent %lf and got %lf\n",
    rank, msgsent, msgrcvd);
```

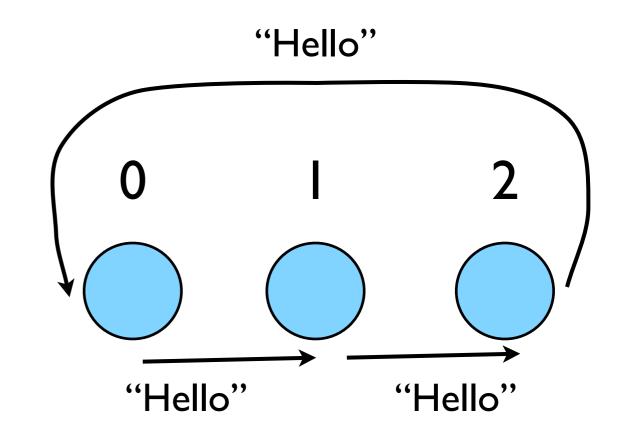
```
ierr = MPI_Finalize();
return 0;
```

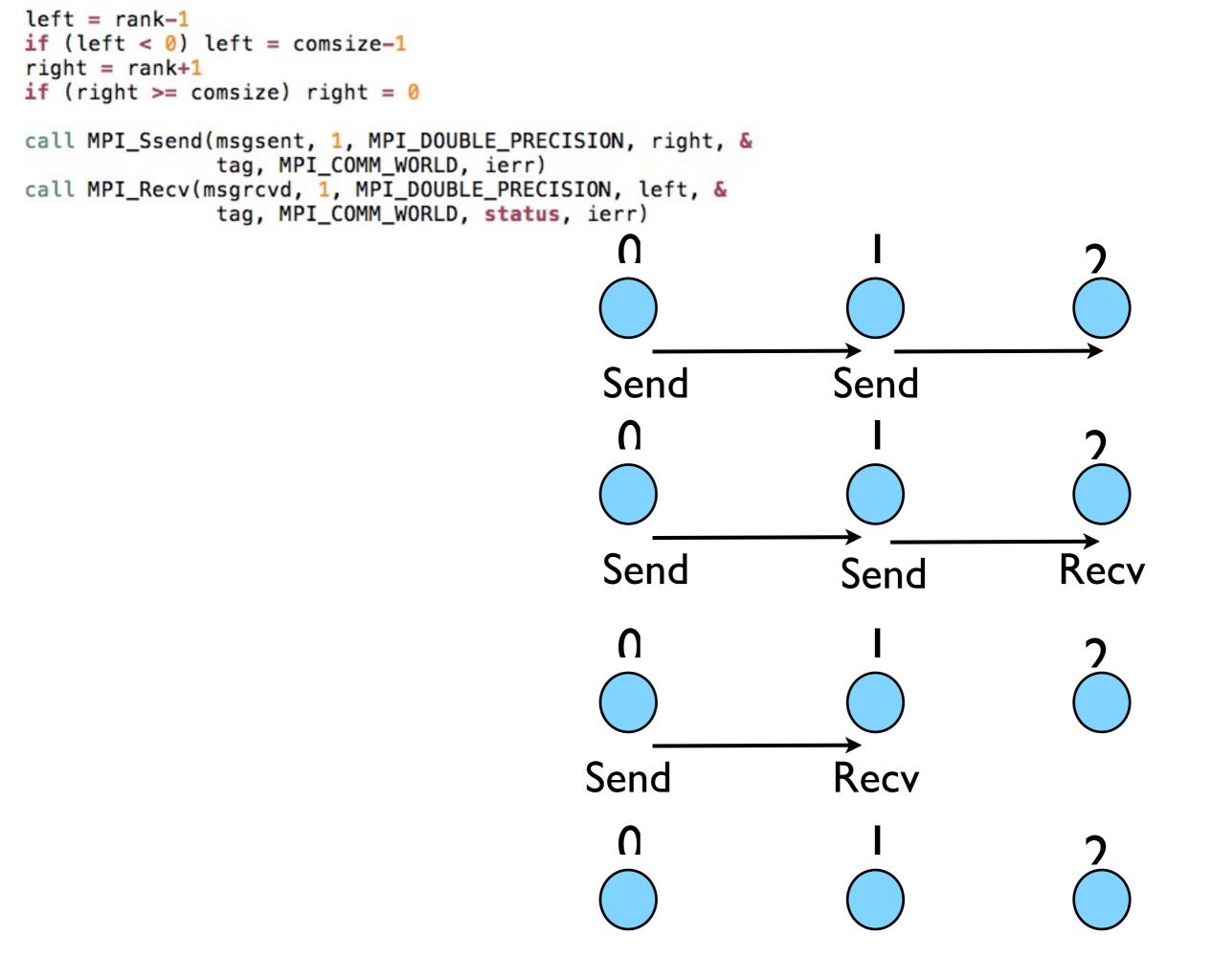
}



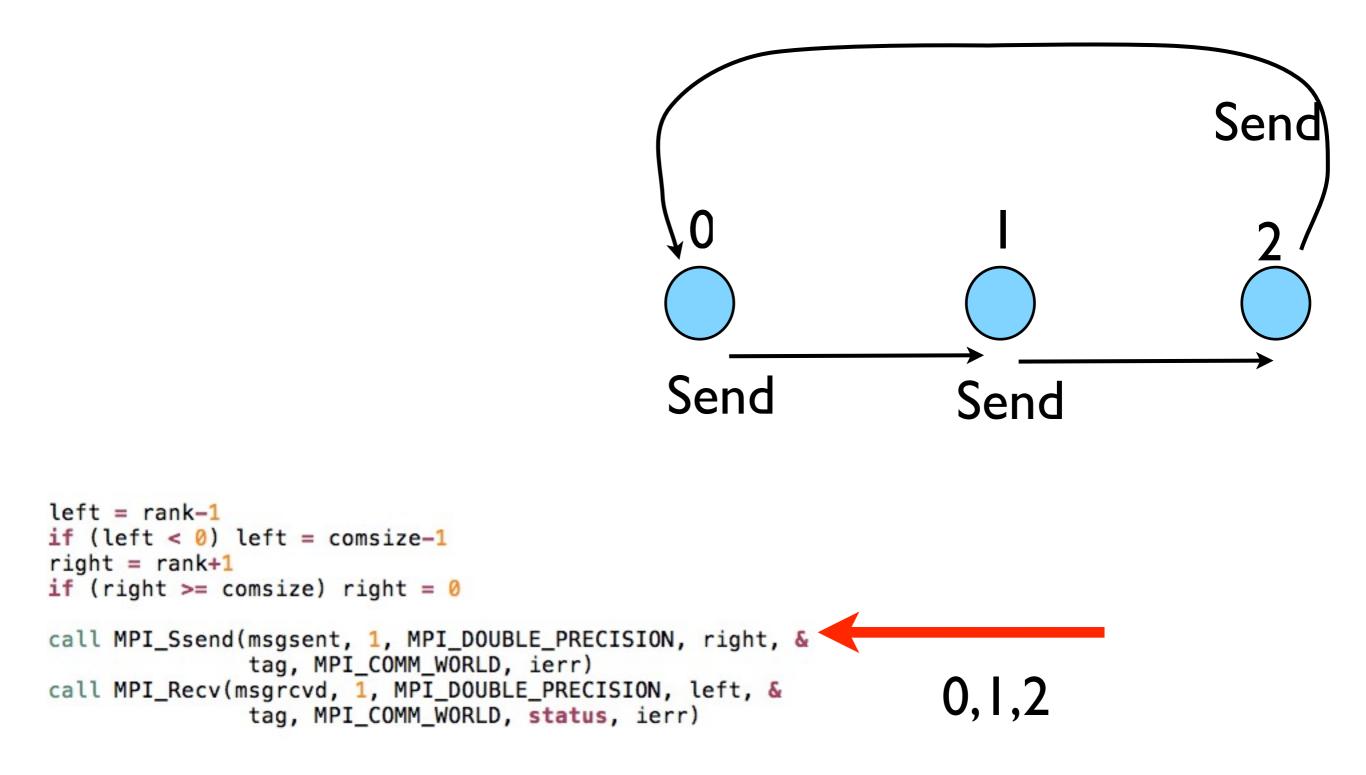
Implement periodic boundary conditions

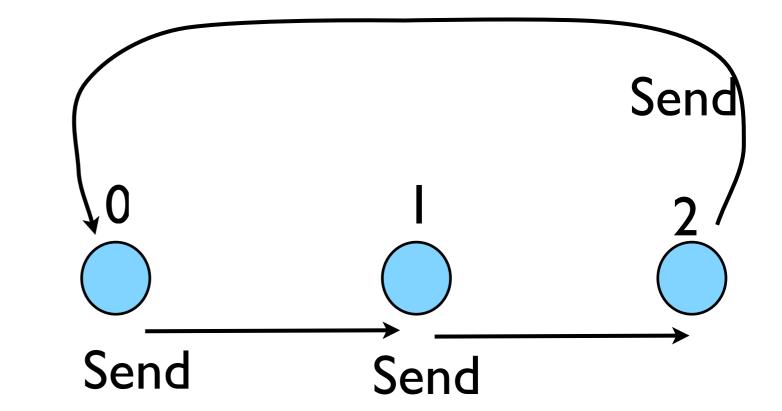
- cp secondmessage.{c,f90}
 thirdmessage.{c,f90}
- edit so it `wraps around'
- mpi{cc,f90} thirdmessage.
 {c,f90} -o thirdmessage
- mpirun -np 3 thirdmessage





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Deadlock

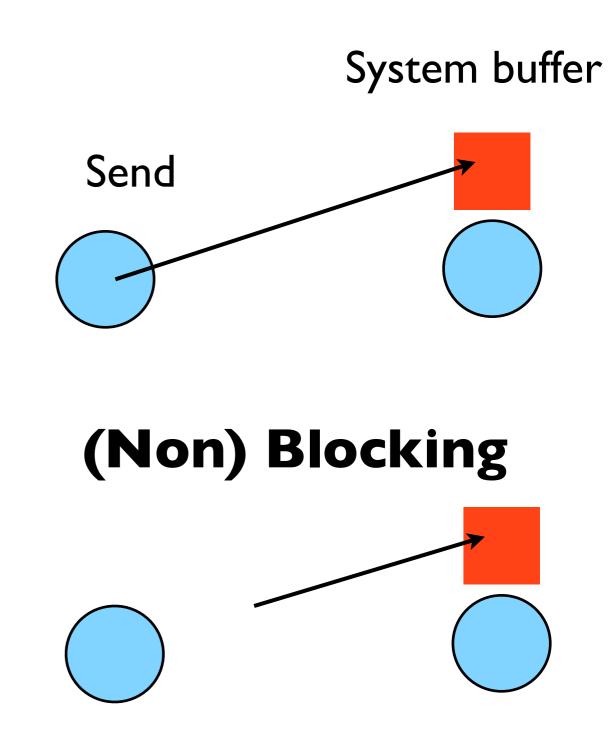
- A classic parallel bug
- Occurs when a cycle of tasks are for the others to finish.
- Whenever you see a closed cycle, you likely have (or risk) deadlock.

Big MPI Lesson #1

All sends and receives must be paired, **at time of sending**

Different versions of SEND

- SSEND: safe send; doesn't return until receive has started. Blocking, no buffering.
- SEND: Undefined. Blocking, probably buffering
- ISEND : Unblocking, no buffering
- IBSEND: Unblocking, buffering

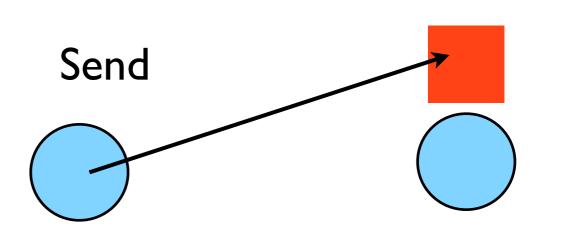


Buffering

Buffering is dangerous!

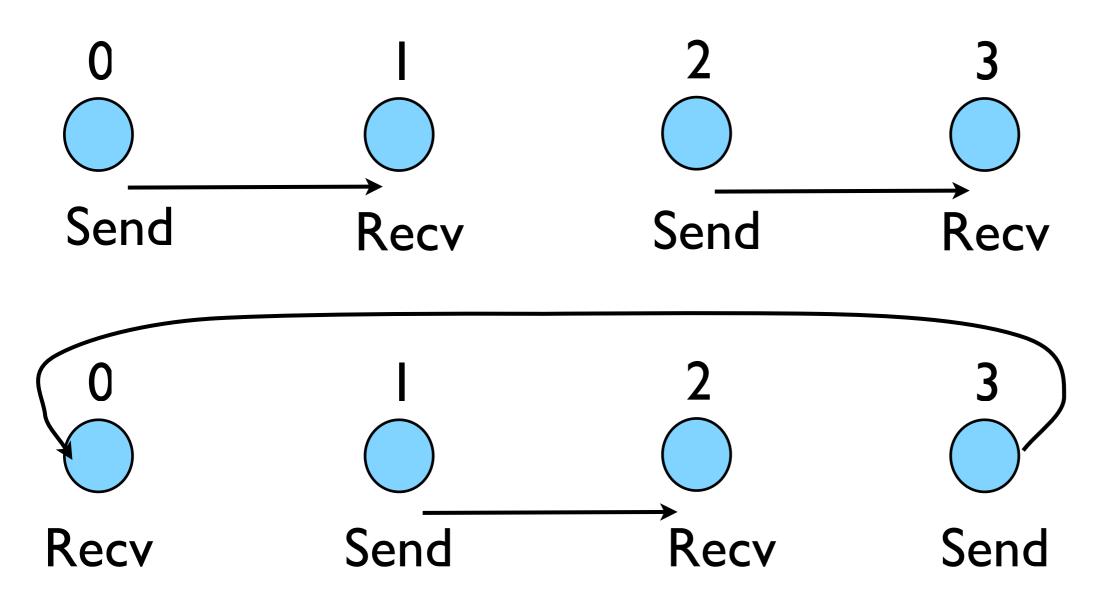
- Worst kind of danger: will usually work.
- Think voice mail; message sent, reader reads when ready
- But voice mail boxes do fill
- Message fails.
- Program fails/hangs mysteriously.
- (Can allocate your own buffers)

Buffering



System buffer

Without using new MPI routines, how can we fix this?



- First: evens send, odds receive
- Then: odds send, evens receive
- Will this work with an odd # of processes?
- How about 2? 1?

```
program fourthmessage
implicit none
include 'mpif.h'
    integer :: ierr, rank, comsize
    integer :: left, right
    integer :: tag
    integer :: status(MPI_STATUS_SIZE)
    double precision :: msgsent, msgrcvd
    call MPI INIT(ierr)
    call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
    call MPI COMM SIZE(MPI COMM WORLD, comsize, ierr)
    left = rank-1
    if (left < 0) left = comsize-1</pre>
    right = rank+1
    if (right >= comsize) right = 0
   msgsent = rank*rank
                                                                       Evens send first
   msgrcvd = -999.
    tag = 1
    if (mod(rank,2) == 0) then
       call MPI_Ssend(msgsent, 1, MPI_DOUBLE_PRECISION, right, &
                      tag, MPI_COMM_WORLD, ierr)
        call MPI_Recv(msgrcvd, 1, MPI_DOUBLE_PRECISION, left, &
                      tag, MPI COMM WORLD, status, ierr)
   else
        call MPI_Recv(msgrcvd, 1, MPI_DOUBLE_PRECISION, left, &
                                                                           Then odds
                      tag, MPI_COMM_WORLD, status, ierr)
       call MPI_Ssend(msgsent, 1, MPI_DOUBLE_PRECISION, right, &
                      tag, MPI_COMM_WORLD, ierr)
   endif
    print *, rank, 'Sent ', msgsent, 'and recvd ', msgrcvd
   call MPI_FINALIZE(ierr)
                                                               fourthmessage.f90
end program fourthmessage
```

```
#include <stdio.h>
#include <mpi.h>
int main(int argc, char **argv) {
   int rank, size, ierr;
   int left, right;
   int tag=1;
   double msgsent, msgrcvd;
   MPI_Status rstatus;
    ierr = MPI_Init(&argc, &argv);
    ierr = MPI_Comm_size(MPI_COMM_WORLD, &size);
    ierr = MPI_Comm_rank(MPI_COMM_WORLD, &rank);
    left = rank -1;
   if (left < 0) left = size-1;</pre>
    right = rank + 1;
   if (right == size) right = 0;
   msgsent = rank*rank;
                                                                     Evens send first
   msgrcvd = -999;
   if (rank % 2 == 0) {
        ierr = MPI_Ssend(&msgsent, 1, MPI_DOUBLE, right,
                        tag, MPI_COMM_WORLD);
        ierr = MPI_Recv(&msgrcvd, 1, MPI_DOUBLE, left,
                        tag, MPI_COMM_WORLD, &rstatus);
   } else {
        ierr = MPI_Recv(&msgrcvd, 1, MPI_DOUBLE, left,
                        tag, MPI_COMM_WORLD, &rstatus);
                                                                            Then odds
        ierr = MPI_Ssend(&msgsent, 1, MPI_DOUBLE, right,
                        tag, MPI_COMM_WORLD);
    }
   printf("%d: Sent %lf and got %lf\n",
               rank, msgsent, msgrcvd);
                                                               fourthmessage.c
    ierr = MPI_Finalize();
    return 0;
}
```

Something new: Sendrecv

- A blocking send and receive built in together
- Lets them happen simultaneously
- Can automatically pair the sends/recvs!
- dest, source does not have to be same; nor do types or size.

```
#include <stdio.h>
#include <mpi.h>
int main(int argc, char **argv) {
    int rank, size, ierr;
    int left, right;
    int tag=1;
    double msgsent, msgrcvd;
   MPI_Status rstatus;
    ierr = MPI_Init(&argc, &argv);
    ierr = MPI_Comm_size(MPI_COMM_WORLD, &size);
    ierr = MPI_Comm_rank(MPI_COMM_WORLD, &rank);
    left = rank -1;
    if (left < 0) left = size-1;</pre>
    right = rank + 1;
    if (right == size) right = 0;
   msgsent = rank*rank;
   msgrcvd = -999;
    ierr = MPI_Sendrecv(&msgsent, 1, MPI_DOUBLE, right, tag,
                        &msgrcvd, 1, MPI_DOUBLE, left,
                                                        tag,
                        MPI_COMM_WORLD, &rstatus);
   printf("%d: Sent %lf and got %lf\n",
                rank, msgsent, msgrcvd);
    ierr = MPI_Finalize();
    return 0;
7
                    fifthmessage.c
```

Something new: Sendrecv

- A blocking send and receive built in together
- Lets them happen simultaneously
- Can automatically pair the sends/recvs!
- dest, source does not have to be same; nor do types or size.

```
program fifthmessage
implicit none
include 'mpif.h'
integer :: ierr, rank, comsize
integer :: left, right
integer :: tag
integer :: status(MPI_STATUS_SIZE)
double precision :: msgsent, msgrcvd
call MPI_INIT(ierr)
call MPI_COMM_RANK(MPI_COMM_WORLD, rank, ierr)
call MPI_COMM_SIZE(MPI_COMM_WORLD, comsize, ierr)
left = rank-1
if (left < 0) left = comsize-1</pre>
right = rank+1
if (right >= comsize) right = 0
msgsent = rank*rank
msqrcvd = -999.
tag = 1
call MPI_Sendrecv(msgsent, 1, MPI_DOUBLE_PRECISION, right, tag, &
                  msgrcvd, 1, MPI_DOUBLE_PRECISION, left, tag, &
                  MPI_COMM_WORLD, status, ierr)
print *, rank, 'Sent ', msgsent, 'and recvd ', msgrcvd
call MPI_FINALIZE(ierr)
end program fifthmessage
                     fifthmessage.f90
```

Sendrecv = Send + Recv

C syntax

MPI_Status status; Send Args

Recv Args

FORTRAN syntax

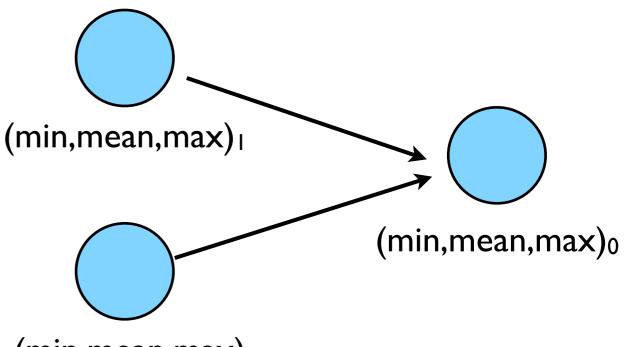
integer status(MPI_STATUS_SIZE)

call MPI_SENDRECV (sendptr, count, MPI_TYPE, destination,tag, recvptr, count, MPI_TYPE, source, tag, Communicator, status, ierr)

Why are there two different tags/types/counts?

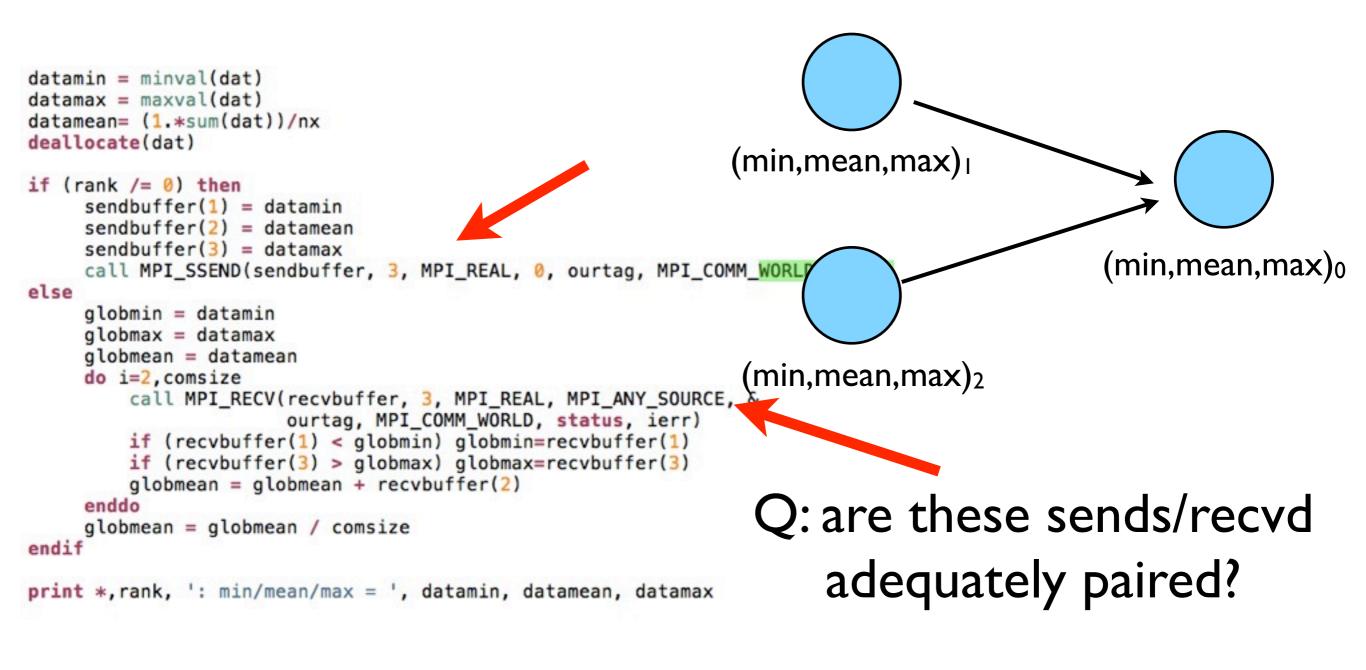
Min, Mean, Max of numbers

- Lets try some code that calculates the min/mean/max of a bunch of random numbers -1..1. Should go (min,mean,max)₂ to -1,0,+1 for large N.
- Each gets their partial results and sends it to some node, say node 0 (why node 0?)
- ~/ppp/mpi-intro/minmeanmax. {c,f90}
- How to MPI it?

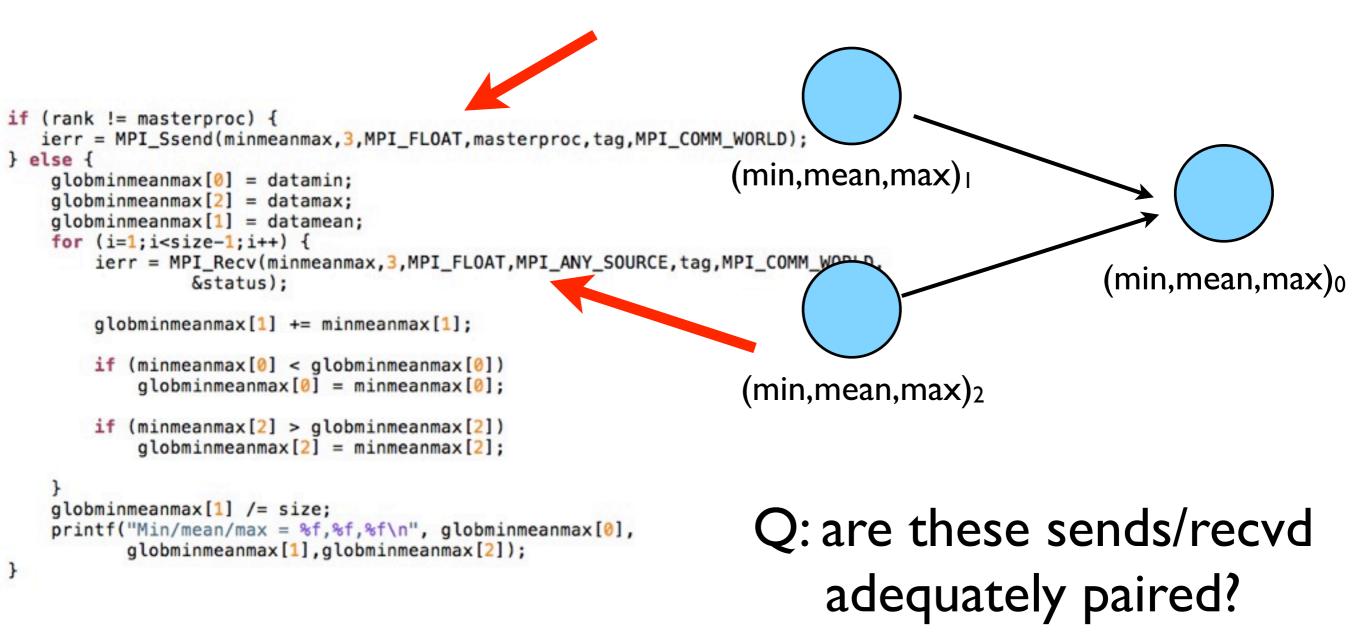


```
program randomdata
       implicit none
       integer,parameter :: nx=1500
       real, allocatable :: dat(:)
       integer :: i
       real :: datamin, datamax, datamean
!
! random data
!
       allocate(dat(nx))
       call random_seed(put=[(i,i=1,8)])
       call random_number(dat)
       dat = 2*dat - 1.
!
! find min/mean/max
1
       datamin = minval(dat)
       datamax = maxval(dat)
       datamean= (1.*sum(dat))/nx
       deallocate(dat)
       print *, 'min/mean/max = ', datamin, datamean, datamax
       return
       end
```

```
/*
 * generate random data
 */
dat = (float *)malloc(nx * sizeof(float));
srand(0);
for (i=0;i<nx;i++) {</pre>
    dat[i] = 2*((float)rand()/RAND_MAX)-1.;
}
/*
 * find min/mean/max
*/
datamin = 1e+19;
datamax =-1e+19;
datamean = 0;
for (i=0;i<nx;i++) {</pre>
    if (dat[i] < datamin) datamin=dat[i];</pre>
    if (dat[i] > datamax) datamax=dat[i];
    datamean += dat[i];
}
datamean /= nx;
free(dat);
printf("Min/mean/max = %f,%f,%f\n", datamin,datamean,datamax);
```



minmeanmax-mpi.f90

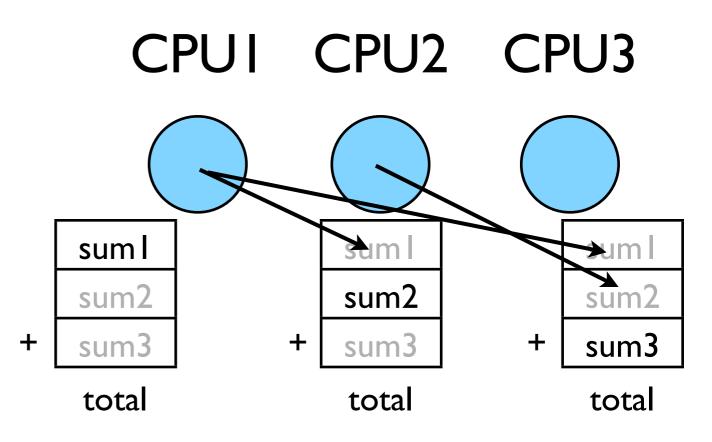


minmeanmax-mpi.c

Inefficient!

Requires (P-I) messages, 2

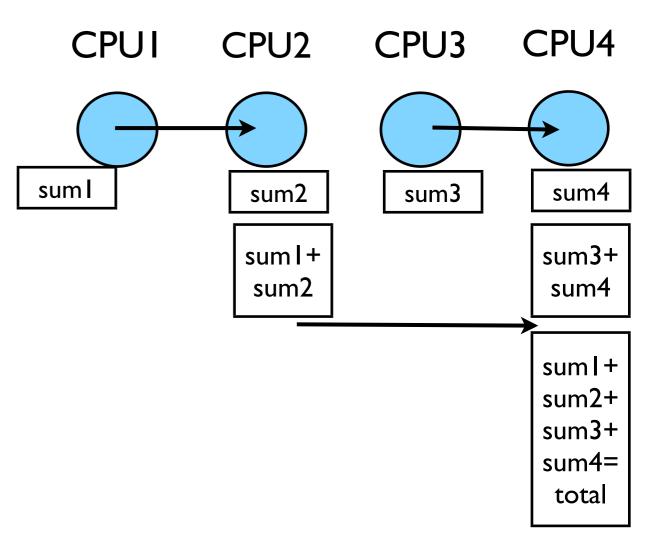
 (P-I) if everyone then needs
 to get the answer.



Better Summing

- Pairs of processors; send partial sums
- Max messages received log₂(P)
- Can repeat to send total back

 $T_{\rm comm} = 2\log_2(P)C_{\rm comm}$



Reduction; works for a variety of operators (+,*,min,max...)

```
print *, rank, ': min/mean/max = ', datamin, datamean, datamax
```

combine data



to just send to task 0:

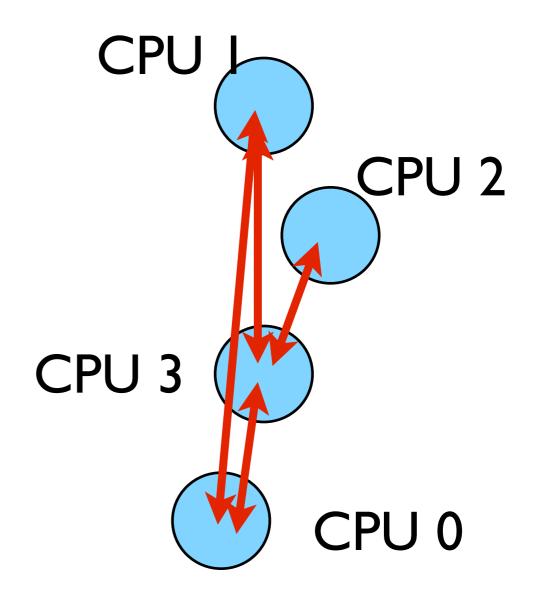
MPI_Reduce and MPI_Allreduce

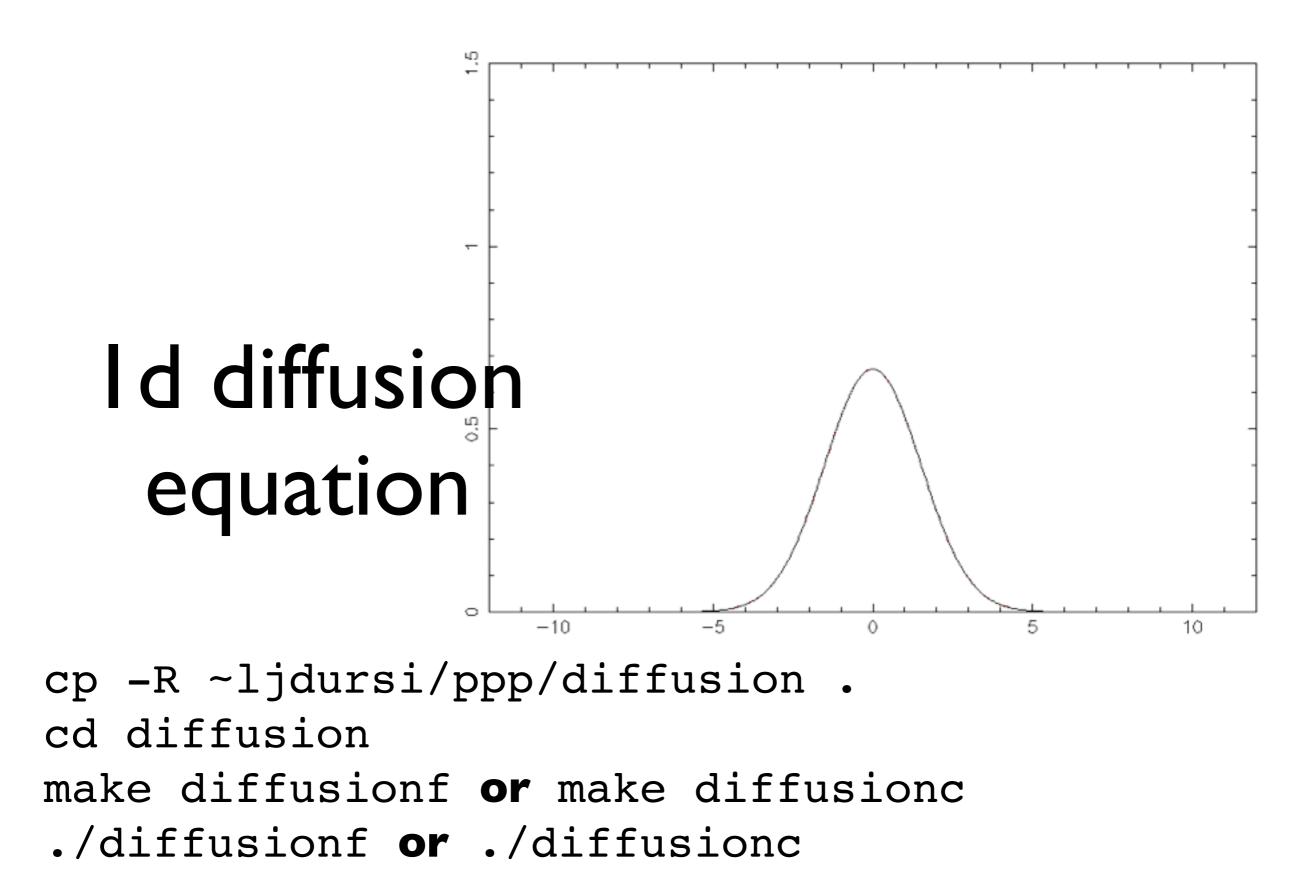
Performs a reduction and sends answer to one PE (Reduce) or all PEs (Allreduce)

minmeanmax-allreduce.f

Collective Operations

- As opposed to the pairwise messages we've seen
- All processes in the communicator must participate
- Cannot proceed until all have participated
- Don't necessarily know what goes on 'under the hood'

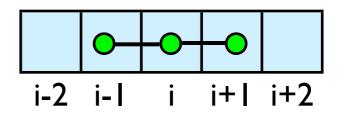


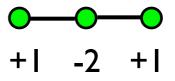


Discretizing Derivatives

- Done by finite differencing the discretized values
- Implicitly or explicitly involves interpolating data and taking derivative of the interpolant
- More accuracy larger 'stencils'

$$\left. \frac{d^2 Q}{dx^2} \right|_i \approx \frac{Q_{i+1} - 2Q_i + Q_{i-1}}{\Delta x^2}$$

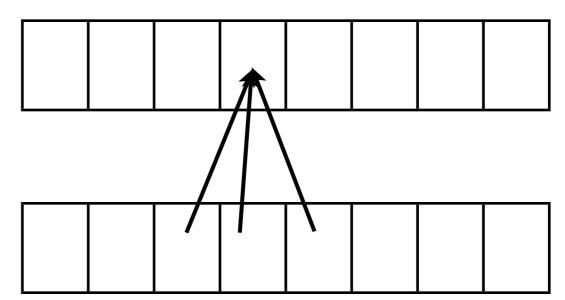




Diffusion Equation

$$\begin{split} \frac{\partial T}{\partial t} &= D \frac{\partial^2 T}{\partial x^2} \\ \frac{\partial T_i^{(n)}}{\partial t} &\approx \frac{T_i^{(n)} + T_i^{(n-1)}}{\Delta t} \\ \frac{\partial T_i^{(n)}}{\partial x} &\approx \frac{T_{i+1}^{(n)} - 2T_i^{(n)} + T_{i-1}^{(n)}}{\Delta x^2} \\ T_i^{(n+1)} &\approx T_i^{(n)} + \frac{D\Delta t}{\Delta x^2} \left(T_{i+1}^{(n)} - 2T_i^{(n)} + T_{i-1}^{(n)}\right) \end{split}$$

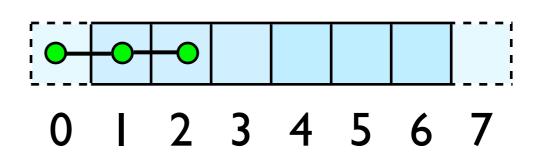
- Simple Id PDE
- Each timestep, new data for T[i] requires old data for T[i+1],T[i],T[i-1]



Guardcells

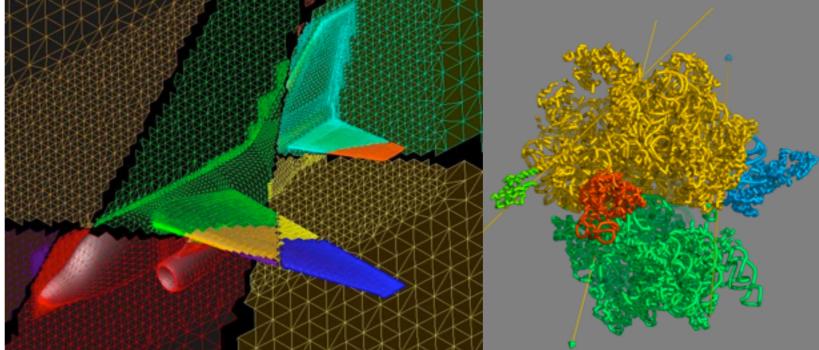
- How to deal with boundaries?
- Because stencil juts out, need information on cells beyond those you are updating
- Pad domain with 'guard cells' so that stencil works even for the first point in domain
- Fill guard cells with values such that the required boundary conditions are met

Global Domain



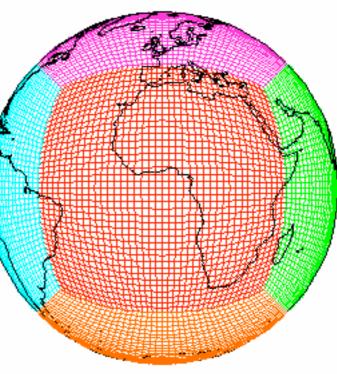
ng = I loop from ng, N - 2 ng

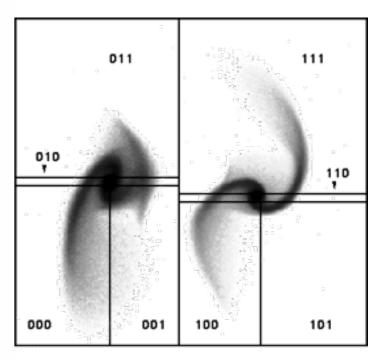
Domain Decomposition



http://adg.stanford.edu/aa241 /design/compaero.html http://www.uea.ac.uk/cmp/research/cmpbio/ Protein+Dynamics,+Structure+and+Function

- A very common approach to parallelizing on distributed memory computers
- Maintain Locality; need local data mostly, this means only surface data needs to be sent between processes.



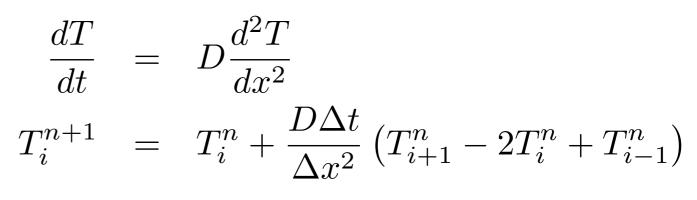


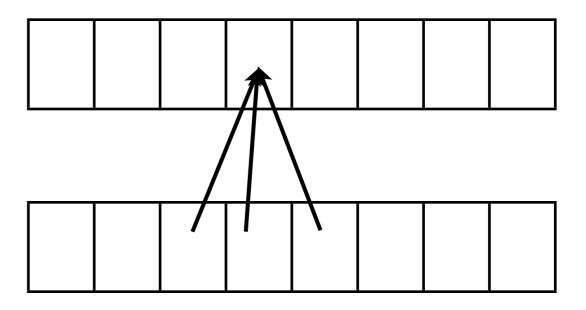
http://sivo.gsfc.nasa.gov /cubedsphere_comp.html

http://www.cita.utoronto.ca/~dubinski /treecode/node8.html

Implement a $\frac{dT}{dt} = D\frac{d^2T}{dx^2}$ diffusion $T_i^{n+1} = T_i^n + \frac{1}{2}$ equation in MPI

 Need one neighboring number per neighbor per timestep

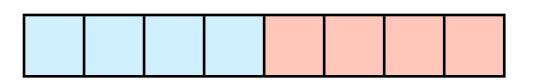


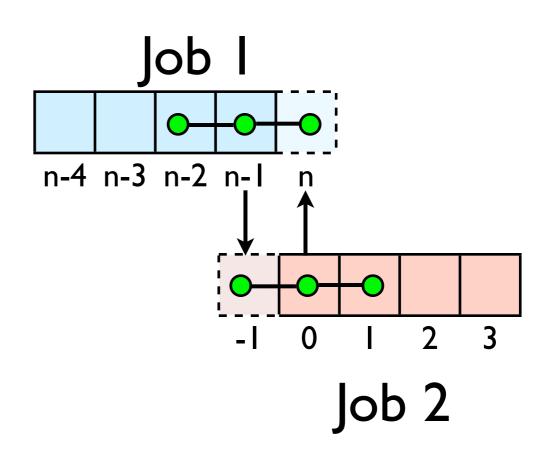


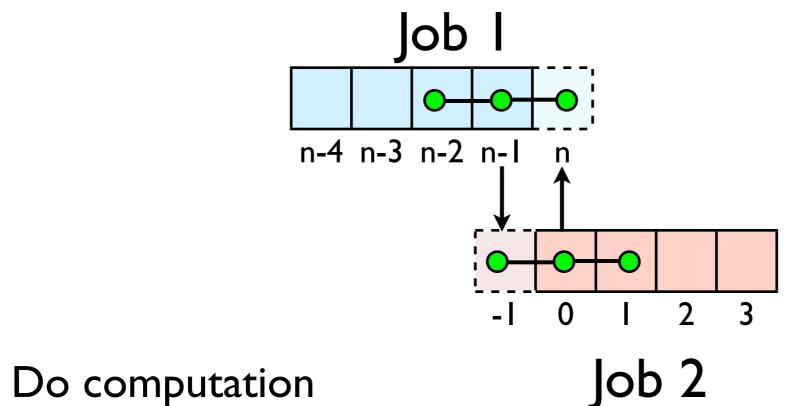
Guardcells

- Works for parallel decomposition!
- Job I needs info on Job 2s 0th zone, Job 2 needs info on Job Is last zone
- Pad array with 'guardcells' and fill them with the info from the appropriate node by message passing or shared memory
- Hydro code: need guardcells 2 deep









- guardcell exchange: each cell has to do 2 sendrecvs
 - its rightmost cell with neighbors leftmost
 - its leftmost cell with neighbors rightmost
 - Everyone do right-filling first, then left-filling (say)
 - For simplicity, start with periodic BCs
 - then (re-)implement fixed-temperature BCs; temperature in first, last zones are fixed

Hands-on: MPI diffusion

- cp diffusionf.f90 diffusionfmpi.f90 or
- cp diffusionc.c diffusionc-mpi.c or
- Make an MPI-ed version of diffusion equation
- (Build: make diffusionf-mpi or make diffusionc-mpi)
- Test on 1..8 procs

- add standard MPI calls: init, finalize, comm_size, comm_rank
- Figure out how many points PE is responsible for (~totpoints/size)
- Figure out neighbors
- Start at I, but end at totpoints/size
- At end of step, exchange guardcells; use sendrecv
- Get total error

C syntax MPI Status status; ierr = MPI Init(&argc, &argv); ierr = MPI Comm {size,rank}(Communicator, &{size,rank}); ierr = MPI Send(sendptr, count, MPI TYPE, destination, tag, Communicator); ierr = MPI Recv(rcvptr, count, MPI_TYPE, source, tag, Communicator, &status); ierr = MPI Sendrecv(sendptr, count, MPI TYPE, destination, tag, recvptr, count, MPI TYPE, source, tag, Communicator, &status); ierr = MPI Allreduce(&mydata, &globaldata, count, MPI TYPE, MPI OP, Communicator);

Communicator -> MPI_COMM_WORLD MPI_Type -> MPI_FLOAT, MPI_DOUBLE, MPI_INT, MPI_CHAR... MPI_OP -> MPI_SUM, MPI_MIN, MPI_MAX,...

FORTRAN syntax

integer status(MPI_STATUS_SIZE)

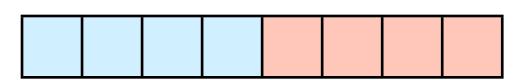
Communicator -> MPI_COMM_WORLD MPI_Type -> MPI_REAL, MPI_DOUBLE_PRECISION, MPI_INTEGER, MPI_CHARACTER MPI_OP -> MPI_SUM, MPI_MIN, MPI_MAX,...

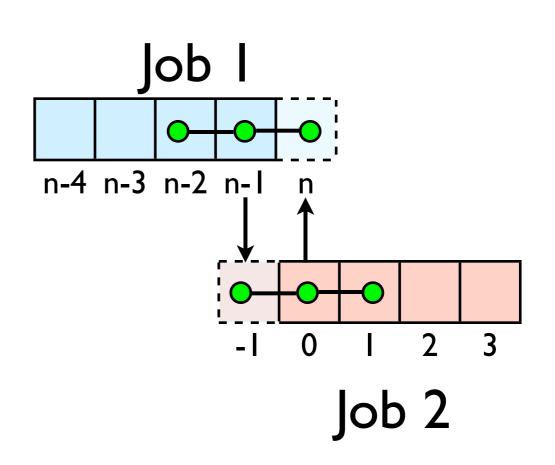
Non-blocking communications

Diffusion: Had to wait for communications to compute

- Could not compute end points without guardcell data
- All work halted while all communications occurred
- Significant parallel overhead

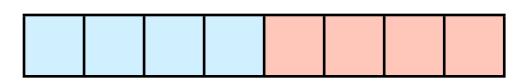




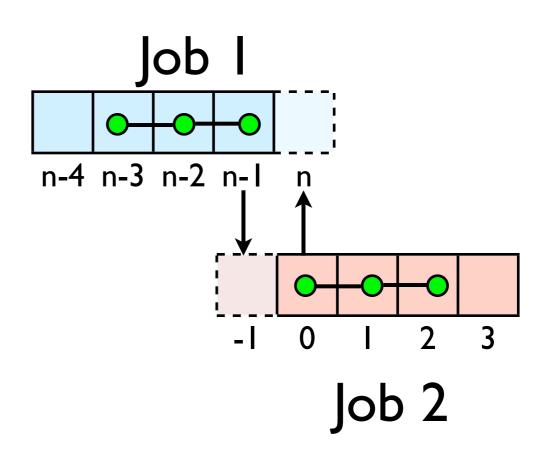


Diffusion: Had to wait?





- But inner zones could have been computed just fine
- Ideally, would do inner zones work while communications is being done; then go back and do end points.



Nonblocking Sends

- Allows you to get work done while message is 'in flight'
- Must **not** alter send buffer until send has completed.
- C:MPI_Isend(void *buf, int count, MPI_Datatype datatype, int dest, int tag, MPI_Comm comm, MPI_Request *request)
- FORTRAN: MPI_ISEND(BUF, INTEGER COUNT, INTEGER DATATYPE, INTEGER DEST, INTEGER TAG, INTEGER COMM, INTEGER REQUEST, INTEGER IERROR)

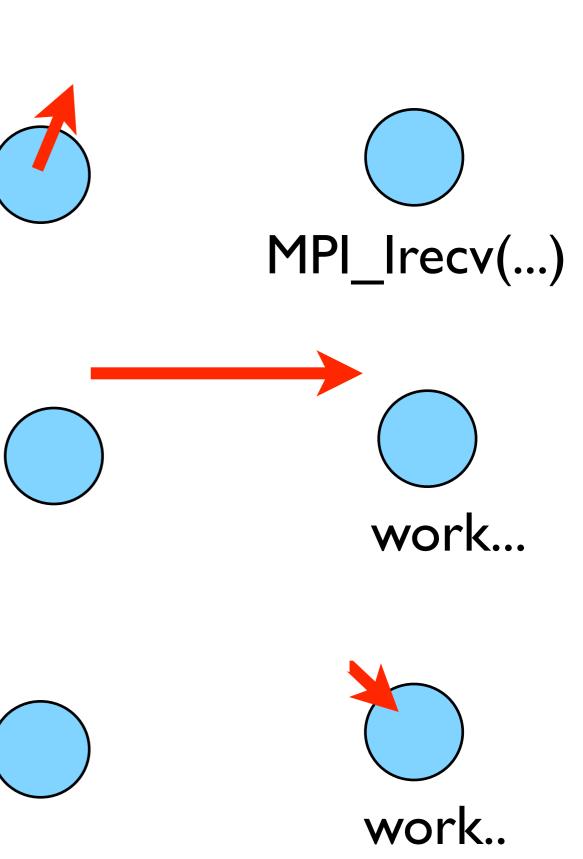
MPI_lsend(...)

work...

work..

Nonblocking Recv

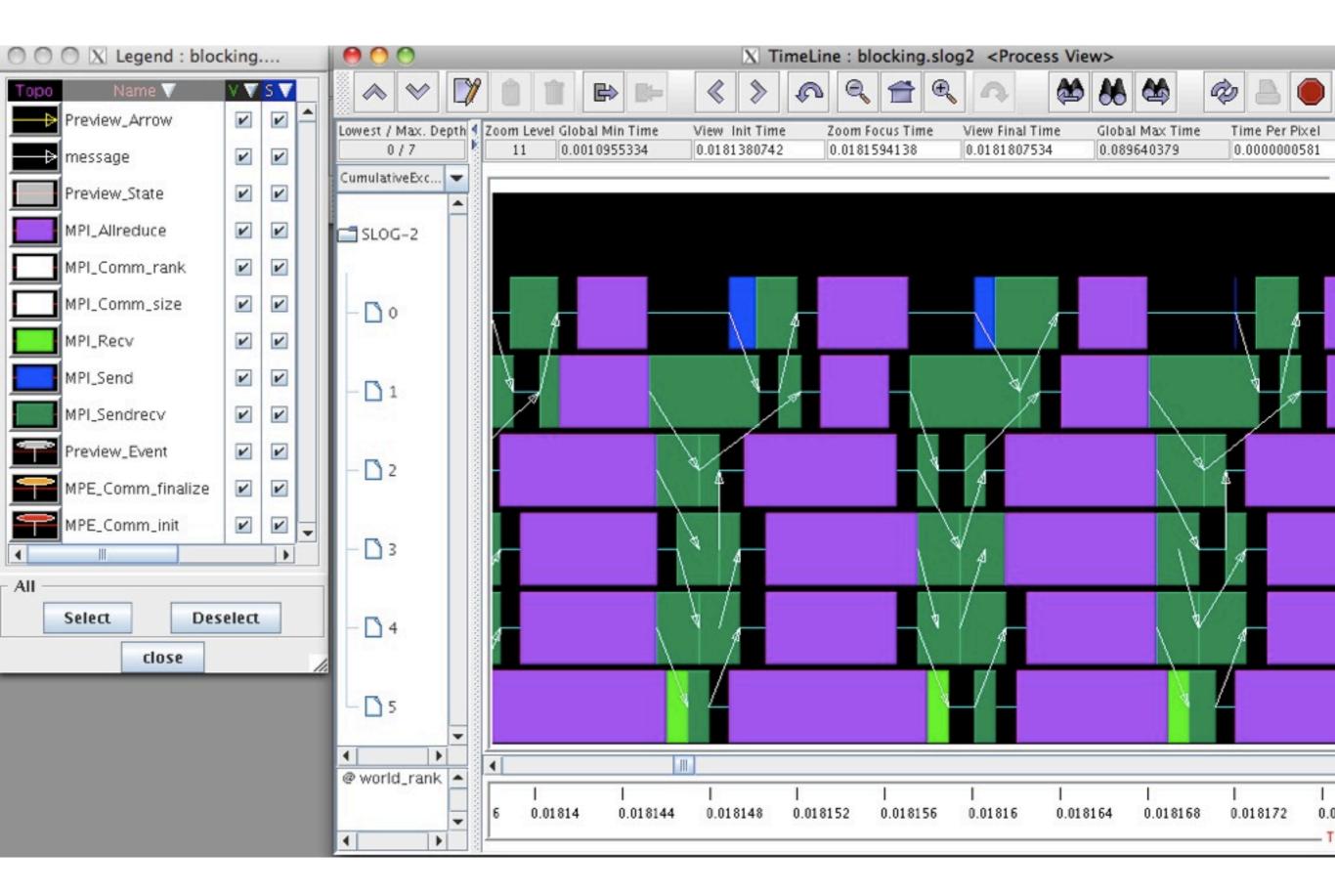
- Allows you to get work done while message is 'in flight'
- Must **not** access recv buffer until recv has completed.
- C:MPI_Irecv(void *buf, int count, MPI_Datatype datatype, int source, int tag, MPI_Comm comm, MPI_Request *request)
- FORTRAN: MPI_IREV(BUF, INTEGER COUNT, INTEGER DATATYPE, INTEGER SOURCE, INTEGER TAG, INTEGER COMM, INTEGER REQUEST, INTEGER IERROR)

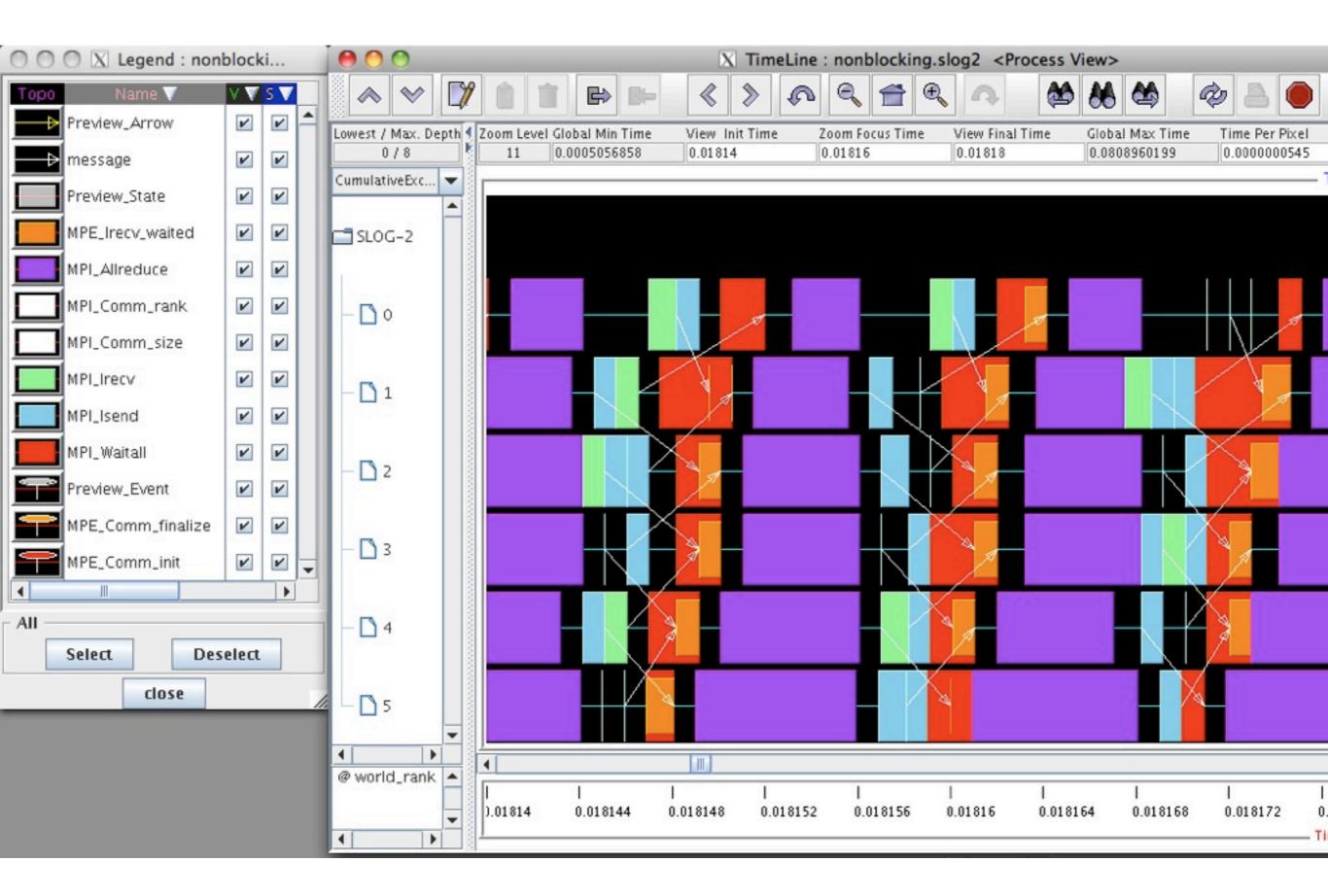


How to tell if message is completed?

- int MPI_Wait(MPI_Request *request,MPI_Status
 *status);
- MPI_WAIT(INTEGER REQUEST,INTEGER STATUS (MPI_STATUS_SIZE),INTEGER IERROR)
- int MPI_Waitall(int count, MPI_Request *array_of_requests, MPI_Status *array_of_statuses);
- MPI_WAITALL(INTEGER COUNT, INTEGER ARRAY_OF_ REQUESTS(*), INTEGER ARRAY_OF_STATUSES (MPI_STATUS_SIZE,*), INTEGER IERROR)

Also: MPI_Waitany, MPI_Test...





Hands On

- In diffusion directory, cp diffusion{c,f}-mpi.{c,f90} to diffusion{c,f}-mpi-nonblocking.{c,f90}
- Change to do non-blocking IO; post sends/recvs, do inner work, wait for messages to clear, do end points